Challenges in fluid, hybrid, and kinetic simulation of Heliophysics phenomena

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• About nomenclature: *scales*

- Brief reminder of what are fluid, hybrid, and kinetic descriptions
- Modelling space plasmas with different plasma descriptions
- Example of scale coupling
- Challenges and future of modelling



• What do "scales" mean? / Observations

- Nomenclature: Large meso micro. OR: Fluid ion electron.
 - Dimension OR physics? Or both?



SuperDARN radar observations of ionospheric plasma circulation



Cluster observations of current sheet structure around reconnection region (Runov et al., 2005)



MMS observations of electron-only reconnection (Huang et al., 2021)

• What do "scales" mean? / Simulations

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Vlasiator simulation of foreshock – magnetosheath interaction

GUMICS-5 MHD simulation of magnetosphere – ionosphere coupling

Fully kinetic simulation of reconnection (Daughton et al. 2011)



If we were able to make a global magnetospheric simulation

- At "electron scales" (i.e., fully kinetic global simulation), would that be a large-scale simulation? Or a small-scale simulation? Or a meso-scale simulation?
 - Answer is: YES.
- At "fluid scales" (i.e., MHD simulation), would that be a large-scale simulation? Or a smallscale simulation? Or a meso-scale simulation?
 - Answer is: large-scale (or fluid-scale) simulation

Logical deduction of the above is therefore

- In modelling, *scales* are very much a concept based on MHD
- Division to *scales* becomes obsolete when moving beyond MHD
 - Ion-kinetic global simulations are inherently producing ion-kinetic physics at the global scale, even though using the definition of micro meso large *scales* they would be meso- or micro-scale.
 - Satellite observations have always been at electron or ion *scales*, because it is the nature which is being observed. (Is it even possible to make fluid-scale observations?)
- Hence, in modelling, people should not anymore talk about fluid, meso or micro *scales*, but fluid, hybrid, kinetic *physics*, whatever the dimension of the problem is.

What is scale-coupling?

- Phenomena, in which dimensionally large features emerge from electron or ion kinetic physics
 - Prime example: Plasma eruptions (substorms, flares, CMEs)
 - Or: Reconnection initiated by electron or ion physics
- Or phenomena in which large features drive consequences detected in electrons or ions
 - For example: Reconnection driven by external conditions

We do not fundamentally understand scale coupling

- Observations: There are great satellites and satellite constellations, and ground-based instruments, but we can never cover the entire region of interest with observations
- Simulations: Nowadays we have large-scale ion-hybrid simulations, but kinetic (explicit) electrons will be impossible also in the foreseeable future
 - Seem Markidis' work with implicit schemes
- → How to reconcile?

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Different levels of plasma description

- Exact microphysical description
 - follow all particles and calculate the resulting fields
 - practically impossible in plasma
 - useful in strong external fields, e.g., acceleration of individual particles in predescribed fields
- Kinetic theory
 - consider particle distribution functions
 - Boltzmann and Vlasov equations
- Macroscopic theory
 - calculate macroscopic variables (density, flux, pressure, temperature,...) from the kinetic theory
 - several different approaches, e.g., magnetohydrodynamics (MHD)



- All you need in plasma physics: all collective descriptions start from the distribution function, and then make some assumptions relevant to the problem at hand
- **Example, billiards**: When does a ball hit the pocket?
 - **Exact particle description, two balls**: Know the velocity and the angle at which the que ball is hit, the friction, etc, predict the pocket at which the ball lands at time *t*
 - Increase the number of balls? The description is most useful for the final shot.



- All you need in plasma physics: all collective descriptions start from the distribution function, and then make some assumptions relevant to the problem at hand
- **Example, billiards**: When does a ball hit the pocket?
 - **Fluid description**: All balls are tied to each other. You don't have individual balls, but a collection. Average velocity of the collection is known at any given time and place.
 - Pocketing? Perhaps you only know when 1/4th of the total density has vanished.



- All you need in plasma physics: all collective descriptions start from the distribution function, and then make some assumptions relevant to the problem at hand
- **Example, billiards**: When does a ball hit the pocket?
 - **Kinetic description**: Make a grid, record the number of balls and their velocity vector in all grid points at all times. Do not follow individual balls.
 - Pocketing? Record the number of balls in pocket grids. Powerful, but costly.



- All you need in plasma physics: all collective descriptions start from the distribution function, and then make some assumptions relevant to the problem at hand
- **Example, billiards**: When does a ball hit the pocket?
 - **Kinetic particle-in-cell description**: Make a grid, create collection of (macro)particles, follow them. At each time *t* reconstruct a distribution function in each grid point.
 - Pocketing? Record a macro particle in pocket grids. Less costly. Detection of pocketings?



Distribution function *f(r,v,t)* is defined in 6D phase space



From *f* to average bulk parameters

How to get macroscopic, measurable parameters (density, temperature etc) from a known distribution function?

A physical quantity related to the given probability distribution is defined as a velocity moment of this distribution

$$n(\mathbf{r},t) = \int f(\mathbf{r},\mathbf{v},t) d^3 v$$

Density is the zeroth moment; $[n] = m^{-3}$

The first moment:

$$\begin{split} \mathbf{\Gamma}_{\alpha}(\mathbf{r},t) &= \int \mathbf{v} f_{\alpha}(\mathbf{r},\mathbf{v},t) d^{3}v & \text{Particle flux; } [\mathbf{\Gamma}] = \mathrm{m}^{-2} \, \mathrm{s}^{-1} \\ \mathbf{V}_{\alpha}(\mathbf{r},t) &= \frac{\int \mathbf{v} f_{\alpha}(\mathbf{r},\mathbf{v},t) d^{3}v}{\int f_{\alpha}(\mathbf{r},\mathbf{v},t) d^{3}v} & \text{Average velocity} = \mathrm{flux/density, } [V] = \mathrm{m} \, \mathrm{s}^{-2} \end{split}$$

Second moment, Pressure tensor

$$\mathcal{P}_{\alpha}(\mathbf{r},t) = m_{\alpha} \int \underbrace{(\mathbf{v} - \mathbf{V}_{\alpha})(\mathbf{v} - \mathbf{V}_{\alpha})}_{\mathbf{v}} f_{\alpha}(\mathbf{r},\mathbf{v},t) d^{3}v$$

dyadic product \rightarrow tensor

 3^{rd} moment \rightarrow heat flux (temperature x velocity), etc. to higher orders...

Example

If temperature of the plasma is understood by the width of the distribution function, what is the temperature of this distribution function?



Answer is: Temperature is a difficult concept... It is the width only when dealing with Maxwellians (and space plasma is almost never Maxwellian)

Motion of f: Vlasov and Boltzmann equations equation(s) of motion for f



2) As particles are not created nor destroyed, the rate of change is due to flux of particles through the surface of the volume.

Let's define the number flux of particles as Uf. Then rate of change through surface S

If
$$\mathbf{F} \neq \mathbf{F}(\mathbf{v})$$
 $\frac{\partial f}{\partial t} + \nabla \cdot (f\mathbf{U}) = 0 \implies \frac{\partial f}{\partial t} + \mathbf{v} \cdot \frac{\partial f}{\partial \mathbf{r}} + \frac{\mathbf{F}}{m} \cdot \frac{\partial f}{\partial \mathbf{v}} = 0$

Coulomb force and gravitation OK, but the magnetic force is $\, \propto \, q({f v} imes {f B}) \,$

Fortunately
$$\frac{\partial}{\partial \mathbf{v}} \cdot (\mathbf{v} \times \mathbf{B}) = 0$$

 $\Rightarrow \qquad \frac{\partial f}{\partial t} + \mathbf{v} \cdot \frac{\partial f}{\partial \mathbf{r}} + \frac{q}{m} (\mathbf{E} + \mathbf{v} \times \mathbf{B}) \cdot \frac{\partial f}{\partial \mathbf{v}} = 0$ Vlasov equation (VE)

Compare with the **Boltzmann equation** in statistical physics (BE)

$$\frac{\partial f}{\partial t} + \mathbf{v} \cdot \frac{\partial f}{\partial \mathbf{r}} + \frac{\mathbf{F}}{m} \cdot \frac{\partial f}{\partial \mathbf{v}} = \left(\frac{\partial f}{\partial t}\right)_c$$

Boltzmann derived $(\partial f/\partial t)_c$ for strong short-range collisions

In plasmas most collisions are long-range small-angle collisions. They are taken care by the average Lorentz force term

$$\frac{\partial f}{\partial t} + \mathbf{v} \cdot \frac{\partial f}{\partial \mathbf{r}} + \frac{q}{m} (\mathbf{E} + \mathbf{v} \times \mathbf{B}) \cdot \frac{\partial f}{\partial \mathbf{v}} = \left(\frac{\partial f}{\partial t}\right)_c^{\mathbf{v}}$$



Ludwig Boltzmann

large-angle collisions only
e.g., charge vs. neutral

VE is often called collisionless Boltzmann equation

Macroscopic plasma description

Macroscopic plasma theories are fluid theories at different levels

- single fluid (magnetohydrodynamics MHD)
- two-fluid (multifluid, separate equations for electron and ion fluids)
- hybrid (fluid electrons with kinetic ions)

Macroscopic equations can be obtained by taking velocity moments of Boltzmann / Vlasov equations



Taking the *n*th moment of BE/VE introduces terms of order *n* +1 !

This leads to *a closure problem*, open chain of equations that must be terminated by applying some form of physical intuition.

Brief reminder of what are fluid, hybrid, and kinetic descriptions: Summary

- Distribution function is key.
 - It's moments give all measurable plasma parameters
- Fluid description:
 - Underlying assumption is that the distribution function is Maxwellian. Single value for fluid temperature. No particles. Average parameters.
- Kinetic description:
 - All particle species are described by an own distribution function everywhere. Distribution function moments give feedback to long-range forces, which feedback to the distributions for all species.
- Hybrid description:
 - Some species are described by a distribution function. Some are fluid.

Everything depends on the plasma distribution



MHD: Distribution function is not modelled. Single value is used for temperature.





Observations

(THEMIS

spacecraft)

Particle-in-cell (PIC). Distribution is constructed from particle statistics.



Vlasiator: Distribution

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Principle of modelling

Terrestrial weather

- Divide the modelling volume into a grid
- Measure modelled parametres in cell centres (e.g. density velocity)
- Compute how much density goes to neighbour and update neighbour cell average
- Use hydrodynamics and partial differential equations (in this example; pick equations of your taste in your problem)
- Compute faster than density moves in reality → forecast





Global modelling techniques



Computational MHD

Magnetohydrodynamics (MHD)

• Plasma as fluid

Riemann problem in MHD

- 8 waves: 8 eigenvalues of a closed equation set
 - Fast magnetosonic
 - Slow magnetosonic
 - Alfvén velocity
 - Bulk velocity (*entropy wave*)
 - 8th wave: zero (∇·**B**=0)

Finite volume method (FVM)

- Cell averages from neighbors
- Conservative

 ρ_2 $rac{\partial u}{\partial t}$ = 0 (continuity) $u = \begin{pmatrix} \rho \\ \mathbf{p} = \rho \mathbf{v} \\ U \\ \mathbf{B} \end{pmatrix} (mass) (momentum) (energy) (magnetic field)$ $\mathbf{F} = \begin{pmatrix} \rho \mathbf{v} \\ \frac{\mathbf{p}\mathbf{p}}{\rho} + P + \frac{B^2}{2\mu_0} - \frac{1}{\mu_0} \mathbf{B} \mathbf{B} \\ (U + P - \frac{B^2}{2\mu_0}) \frac{\mathbf{p}}{\rho} + \frac{1}{\mu_0} (\mathbf{B} \times \frac{\mathbf{p}}{\rho} \times \mathbf{B}) \\ \mathbf{v} \mathbf{B} - \mathbf{B} \mathbf{v} \end{pmatrix}$

$$U=\frac{P}{\gamma-1}+\frac{1}{2}\rho\mathbf{v}^2+\frac{\mathbf{B}^2}{2\mu_0}$$

Grand Unified Magnetosphere Ionosphere Coupling Simulation (GUMICS @FMI)

Ideal conservative MHD

- Riemann solver
- FVM discretization

Boundary conditions

- Input: Solar wind parameters
 - **B**, **v**, n, T (8 parameters)
- Dipole field
- Ionosphere (MHD inner shell at 3.7Re)

Output parameters

 Plasma parameters and the em field in space and time (min. ~1ms)

Adaptive (cell-by-cell) Cartesian grid

Max 8 Re resolution, min typically 0.25 Re

Subcycling (variable time step)

Other MHD codes, e.g.: LFM / GAMERA; BATS-R-US / SWMF



GUMICS ionosphere

istate20200401_041000.tri: SigmaH / Potential / none, Theta=30, P

Spherical 3D

• 20 height levels

Triangular FEM grid

- Fixed in time
- Refined at oval (~100 km)

Electron density

- EUV (F10.7-based empirical)
- Precipitation
 - Maxwellian source

Output variables

• E, Φ , FAC, Σ_P , Σ_H , Joule heat, precipitation energy





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 πm

 $\varepsilon_{prec} = 1$

Similarities & differences to other global codes

Godunov-type solver (&BATS-R-US)

- Sharp stationary boundaries
- 1st order interpolation
 - Others higher order

Cell-by-cell adaptive

 Others block-adaptive or nonadaptive

Knight relationship

- Parallel electric field between ionosphere and magnetosphere
- Implemented but often set to zero
 - Sub-grid scale physics

Not coupled to dedicated codes No current-dependent resistivity

Storm on 2000/04/06



istate19980328_220500.trl: SigmaP / Potential / none, Theta=30, Phi=120



General remarks: MHD & Inner magnetosphere

Inner magnetospheric physics not ideal MHD

- Overlapping plasma populations, different temperature
- Magnetospheric pressure gradient determines R2 FAC
 - Improve partly by refining the magnetospheric grid



This is why several global MHD simulations couple to a dedicated inner magnetosphere like RCM



Picture: Wikipedia



VL/SI/J

- Global ion-kinetic plasma physics beyond MHD
- Electrons are massless charge-neutralising fluid.

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2D or 3D real space (R)

- Divide real space into grid cells
- Compute **E**, **B** fields
- Input to 3D velocity space
- Ohm's law: Hall + electron pressure gradient

3D velocity space (V)

- Each R space cell contains a 3D velocity space
- Propagate and modify ion distribution function using Vlasov equation
- Couple back to real space to update E, B field

Self consistent

Noise-free multi-temperature physics

- Total number of cells: 10¹²
- Over 10⁵ timesteps

More information: <u>http://helsinki.fi/vlasiator</u> Contact PI: <u>Minna.Palmroth@helsinki.fi</u>

The story



2007: First ERC grant (Starting)2011: 6D Test-Vlasov in MHD fields2012: Access to Europe's supercomputers

- First 5D runs (2D3V)
 2015: Second ERC grant (Consolidator)
 2019: Towards 6D (AMR)
- First preliminary run @CSC2021: (Jan 13)
- First 6D production run @HLRS
- Around 15 MCPUh
- Data per run: ~30 T

2022: Dynamic ionosphere added



1151/J@R

Enabling 6D: In a nutshell



erc

erc

ADVANCED COMPUTING

N EUROPE

- Part of European Centre of Excellence in Code development (EuroHPC).
- See more: Palmroth et al. LRCA 2018, 2025



CSC

Estimated relative performance gains in Vlasiator



UNIVERSITY OF HELSINKI FACULTY OF SCIENCE

Image by Y. Pfau-Kempf

Fully kinetic simulations (kinetic electrons)

- Explicit schemes: local geometries
 - Electron kinetic physics occurs in ~100-1000x smaller scales → real space resolution, time steps
- Implicit schemes: Mercury (e.g., Lapenta et al. JGR 2022)
 - See e.g. Lavorenti PhD thesis <u>https://theses.hal.science/tel-04611766v1</u> about the different schemes
 - Or attend International School/Symposium in Space Simulations (ISSS-16) or similar
- Treating velocity space either through Vlasov (gridded f) or through PIC (follow macroparticles)
 - Own *f* for each population, all influence fields
 - Needs to assume something for the electron and ion mass ratio

Self consistent

Fully kinetic simulation of reconnection (Daughton et al. 2011)



Or: eVlasiator – electron kinetics in hybrid-Vlasov dynamics

Electron distributions globally (Battarbee et al., 2021: https://doi.org/10.5194/ang eo-2020-31)

 Based on ion-determined em-fields

Agreement with spacecraft (MMS): Alho et al., GRL https://doi.org/10.1029/202 2GL098329)

 Suggests that many (most) elecron VDF features are based on ion-scale em-fields!



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Broad review on plasmoid ejection scenarios



- ... and fast flows earthward
- Dipolarisation disrupts the magnetotail current





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Modelling requirements

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Modelling requirements Tail driven by dayside input → Global NENL → Reconnection CD → 3D kinetic instabilities & drifts Modelling efforts so far 3D Global MHD:

- reconnection
- MHD instabilities, no drifts
- 3D Hybrid-kinetic:
 - Now available



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Residual Field [nT]



Ion kinetic instabilities and reconnection work together to release the plasmoid via plasma sheet flapping



Vlasiator suggests reconciliation:

NENL: Reconnection – current disruption – plasmoid

BUT: Current disruption not in the same local time as reconnection **AND NOT** due to fast flows

CD: Current disruption @ transition region – spreads outwards – large-scale reconnection – plasmoid

BUT: CD caused by flapping, which is caused by reconnection

VL/SI/JOR scenario:

- Two reconnection sites @flanks move to centre: plasmoid
- Centre disrupts the current due to current sheet flapping



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Trends in HPC (relative to space physics)

Read also: https://blog.purestorage.com/perspectives/5-trends-shaping-the-future-of-high-performance-computing/

- Europe has an exascale strategy (EuroHPC)
- Future is in heterogeneous computing
- GPU Computing will increase (portability is key)
- HPC accessibility will increase
 - Tools, performance profiling, etc.
- AI will be used to improve HPC
- Modern data storage will be a critical investment

Trends: Portability and future technologies

- Vlasiator currently runs on AMD-64, ARM, RISCV, and PowerPC
- CPU + GPU architectures (with NVIDIA and AMD)
- Ongoing development for scalable vector architectures and European accelerator project (EPAC)
- Sufficient portability for future architectures
 - This was always our strategy!
- Quantum computing? Forward propagation of a physical system isn't suitable on Quantum.

Vlasiator running on Aarch64 (64bit ARM) on our Lead Developer's mobile! Credits: Urs Ganse & Eleanna Asvestari

In summary

- Economic use of space is skyrocketing.
- Our modern way of life is critically dependent on space-based services.
 - -> There is an increasingly strong need to model geospace accurately.
- Computing resources are massively increasing
 - **BUT**: Their use requires special skills in heterogeneous HPC
 - Only those who take up the challenge will be able to use them
- Future need and massive resources will allow versatile first-principles modelling and AI-based fast data analysis.
 - Skills to develop: HPC, GPU, ML
- BTW we are hiring again soon.

Thank you!

Contact: minna.palmroth@helsinki.fi